

# Multiplicity Statistics & Properties across the HR Diagram

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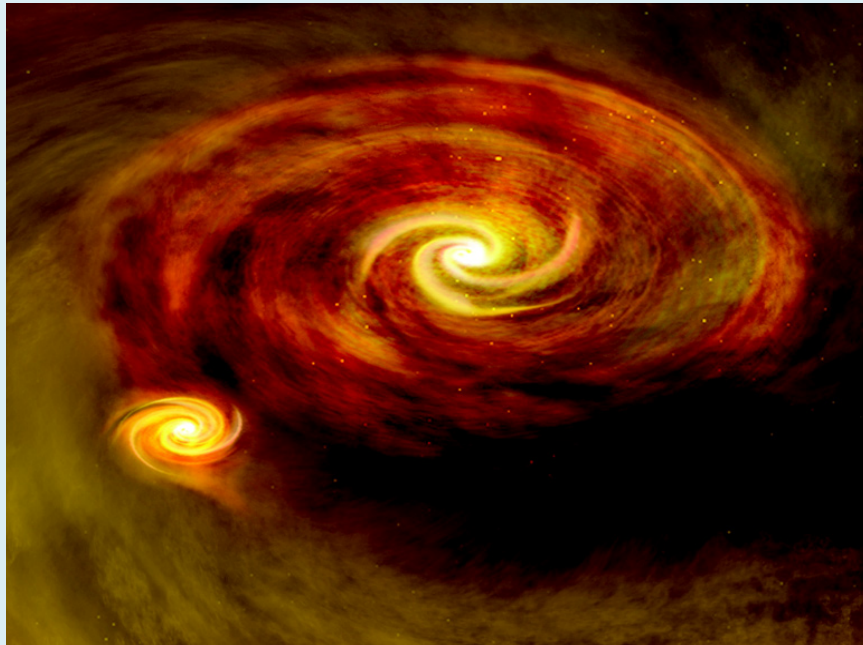
# Overall Theme:

## Two Modes of Binary Star Formation

(Kroupa et al. 1995; Bate et al. 1995, 2002; Kratter et al. 2002, 2006; Clarke 2009; Offner et al. 2010; Lee et al. 2017; **Moe & Di Stefano 2017; Moe et al. 2019**)

Gravitational Instability and  
Fragmentation within **Disk**:

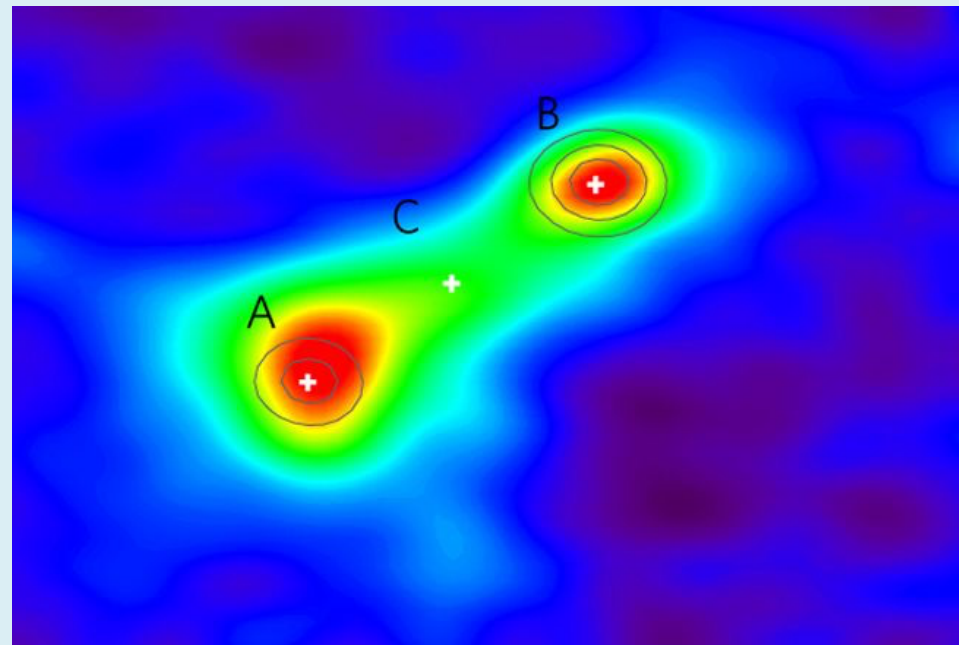
$$Q_{\text{Toomre}} = c_s^2 \Omega / \pi G \Sigma = 3 \alpha c_s^3 / G \dot{M} < 1$$



Close Binaries:  
 $a < 100$  AU

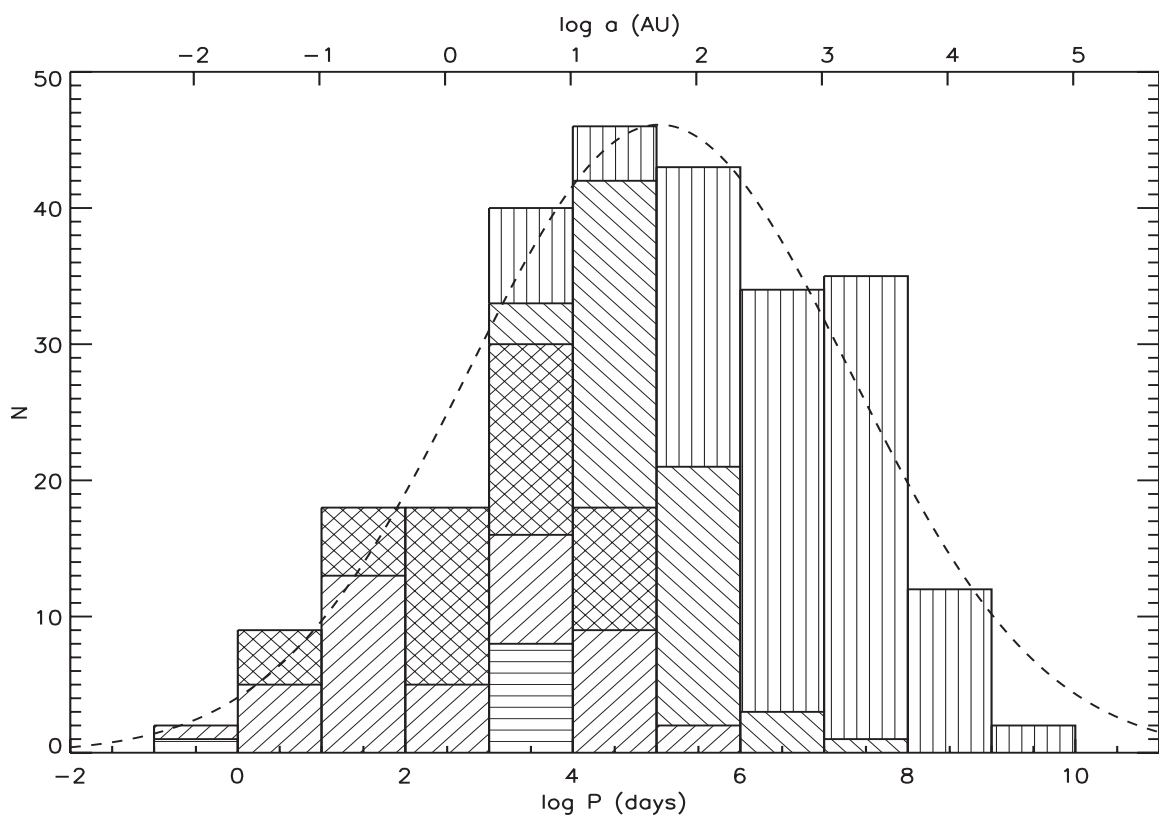
Turbulent Fragmentation  
of Molecular **Cores**:

$$\text{Mach} = \sigma_v / c_s > 1$$



Wide Binaries:  
 $a > 100$  AU

# Field Solar-type Primaries



Duquennoy & Mayor 1991:  
F7-G9 IV/V/VI, ~15 pc

Raghavan et al. 2010:  
F6-K3 IV/V, 25 pc

Tokovinin 2014:  
F0-G9 IV/V, 67 pc

Log-normal period distribution  
peaking at a ~ 50 AU

DM91 measured  $F_{\text{bin}} = 57\%$   
binary fraction, while R10  
and T14 found  $F_{\text{bin}} = 44\%$

Reasons for  $\Delta F_{\text{bin}} = 13\%$  discrepancy:

~3% due to missing late-M companions in R10 (Chini+ 2014; Moe & Di Stefano 2017)

~2% due to sample selection (spectral types, luminosity classes)

~8% due to WD companions added in DM91 (Moe & Di Stefano 2017)

**Gaia will find new WD companions to nearby stars as astrometric binaries.**

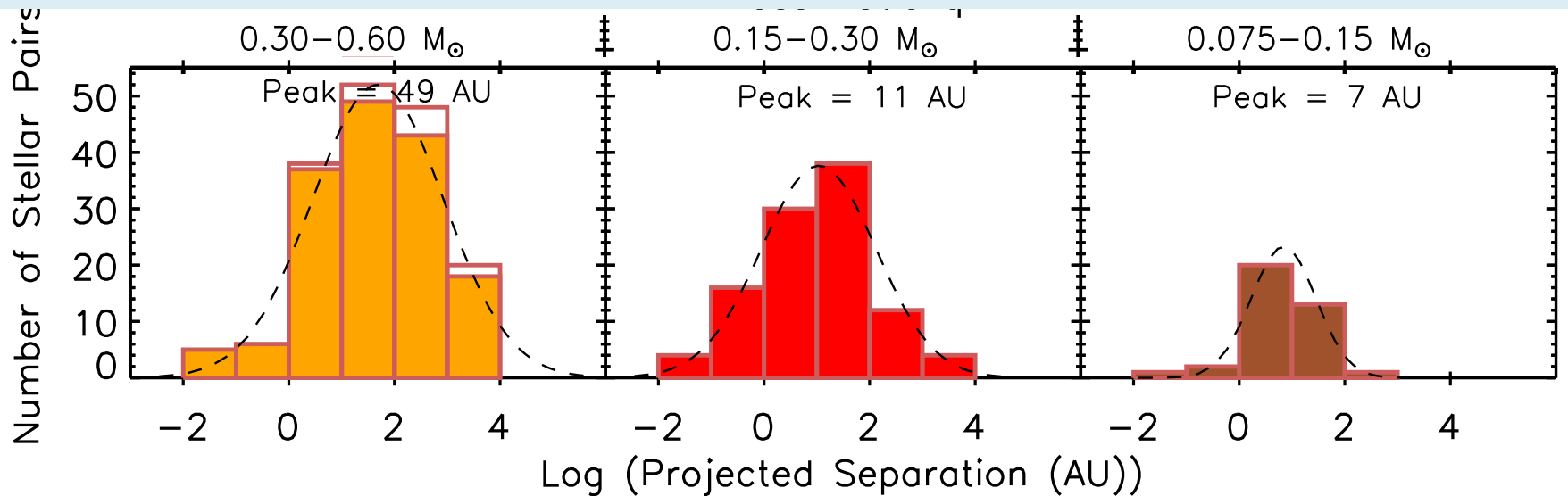
# Field M-dwarf Primaries

Fischer & Marcy 1992; Basri et al. 2006; Law et al. 2008; Bergfors et al. 2010;  
Janson et al. 2012; Dieterich et al. 2012; Ward-Duong et al. 2015;

**Winters et al. 2019, 25 pc,  $M_1 = 0.075 - 0.6 M_\odot$**

Corrected binary fraction of  $F_{\text{bin}} = 27\% \pm 2\%$  for all M-dwarfs,  
increasing from  $F_{\text{bin}} \approx 20\%$  for late-M to  $F_{\text{bin}} \approx 35\%$  for early-M  
(lower than  $F_{\text{bin}} \approx 45\%$  for G-dwarfs)

Log-normal period distribution, peaking at  $a = 50$  AU for early-M  
(similar to G-dwarfs) and  $a = 7$  AU for late-M

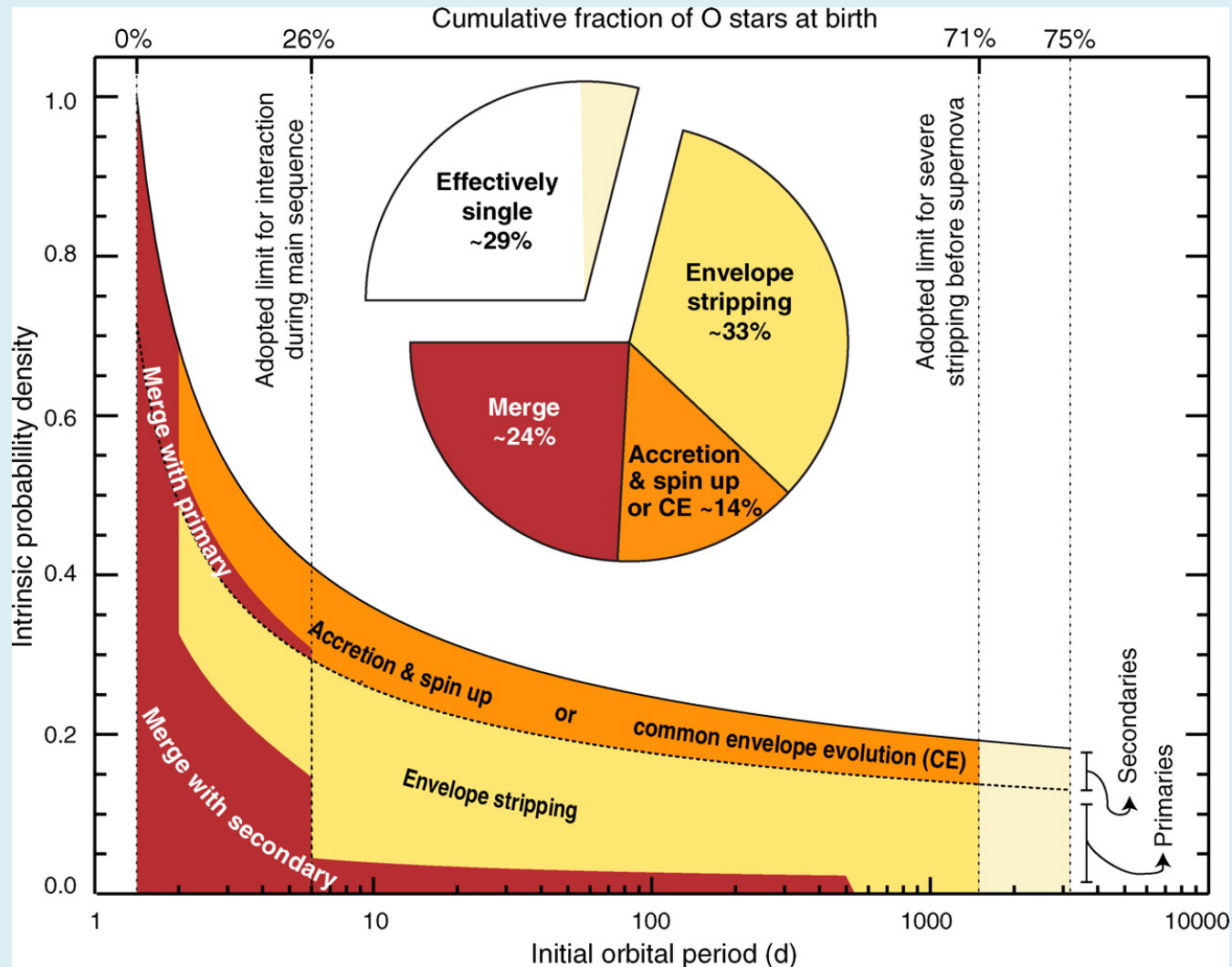


# O-type Primaries

Binary interactions dominate the lives of massive stars (Sana et al. 2012).

~70% of O stars have companions with  $q > 0.1$  within  $a < 10$  AU.

~100% of O stars in clusters (non-runaways) have companions within  $a < 100$  au (Sana et al. 2014; Moe & Di Stefano 2017).

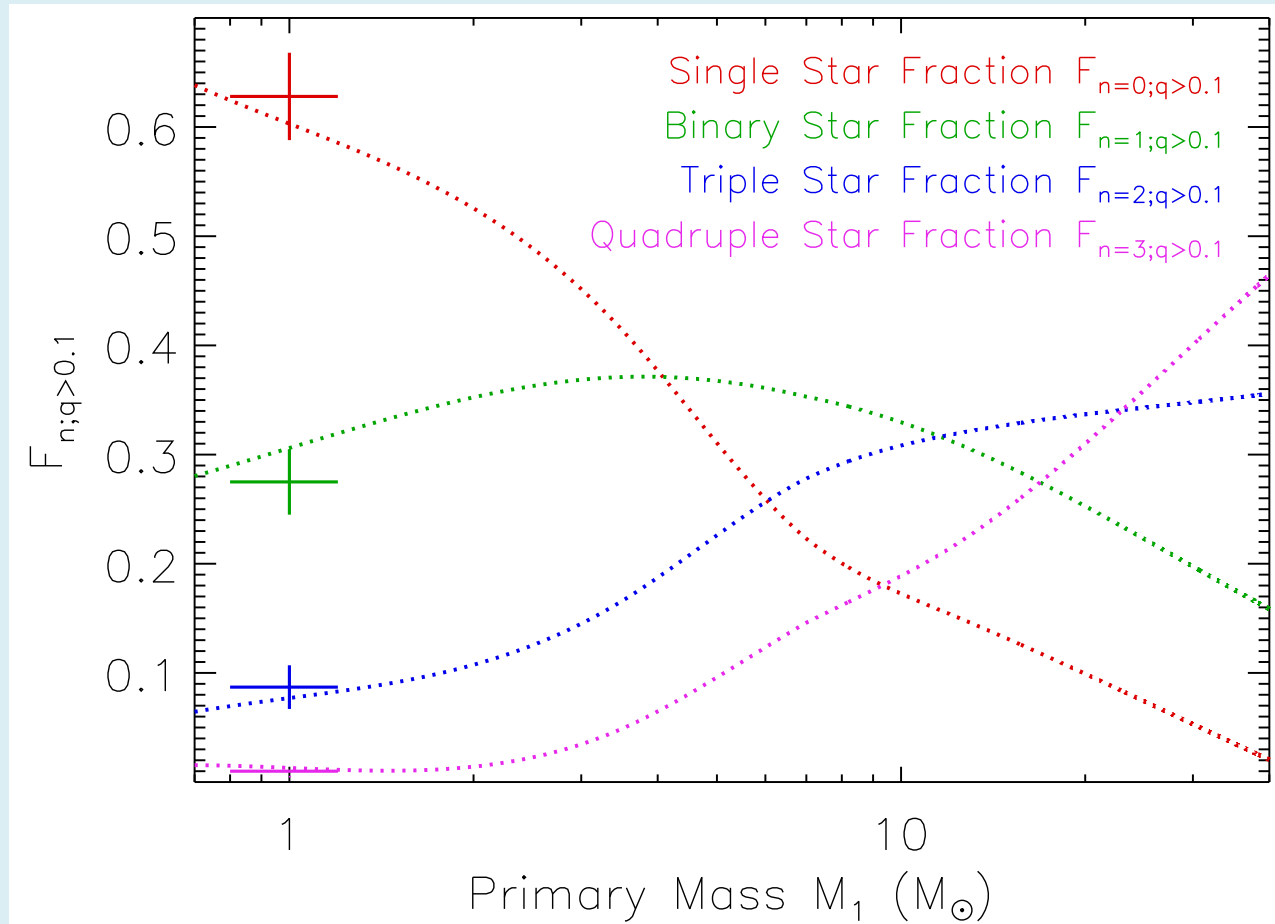


**Gaia can detect  $q < 0.1$  companions to massive stars, and will constrain massive binary properties as a function of age & environment**

# Triple Star Fractions

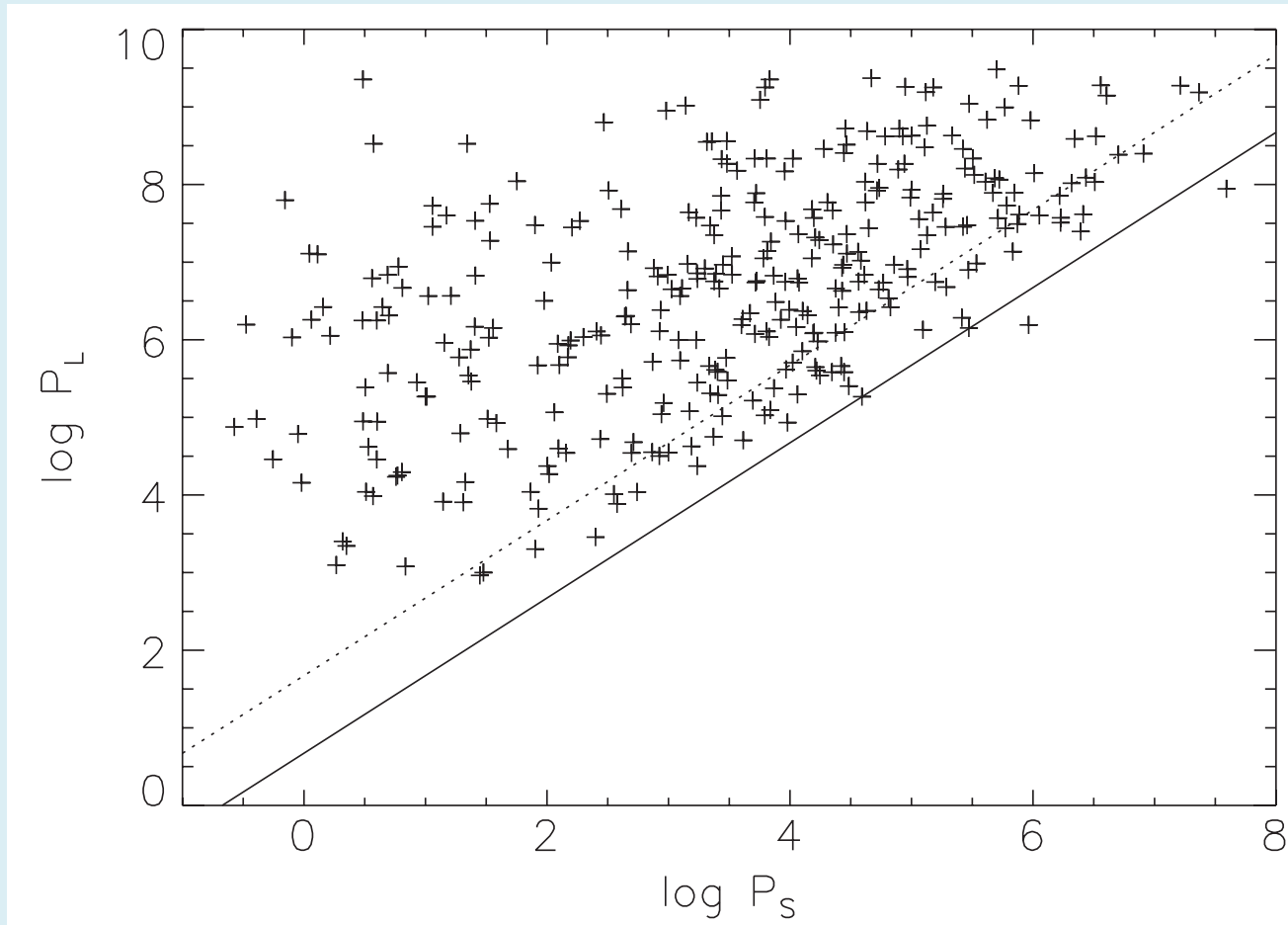
While only 10%-15% of solar-type primaries are in triples (Raghavan et al. 2010; Tokovinin 2014), most massive stars are in triples & higher-ordered multiples (Sana et al. 2014; Moe & Di Stefano 2017)

Every O-type primary has  $2.1 \pm 0.3$  companions with  $q > 0.1$



# Triple Star Hierarchies

Solar-type triples occupy the full parameter space of dynamically stable hierarchies  $f(P_{\text{in}}, P_{\text{out}} > 5 P_{\text{in}})$ , *nearly* consistent with random drawings from overall log-normal period distribution (Tokovinin 2014)

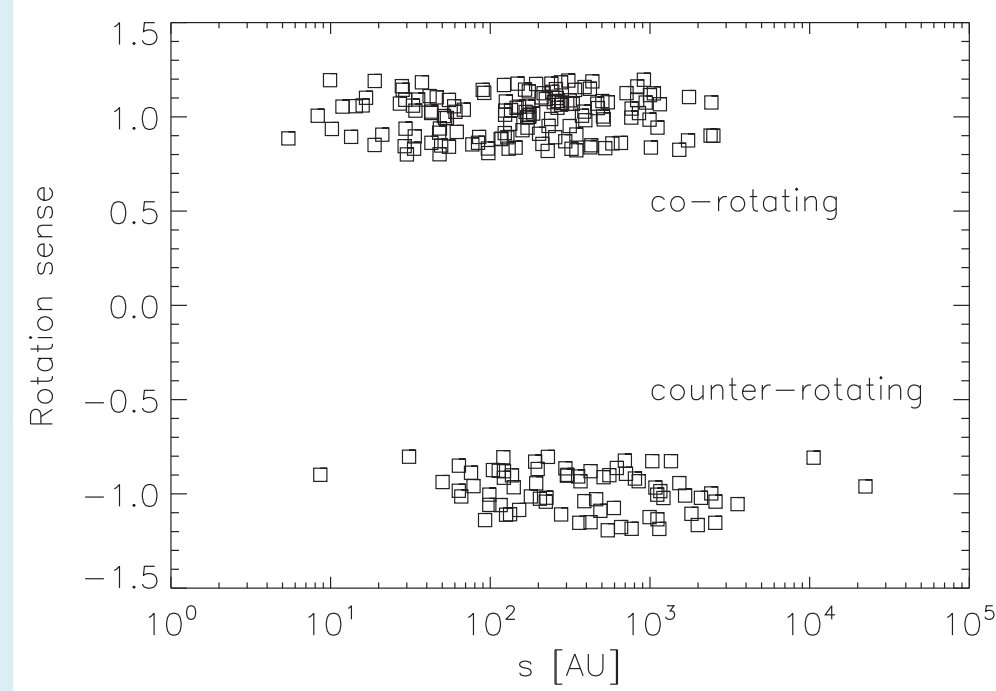
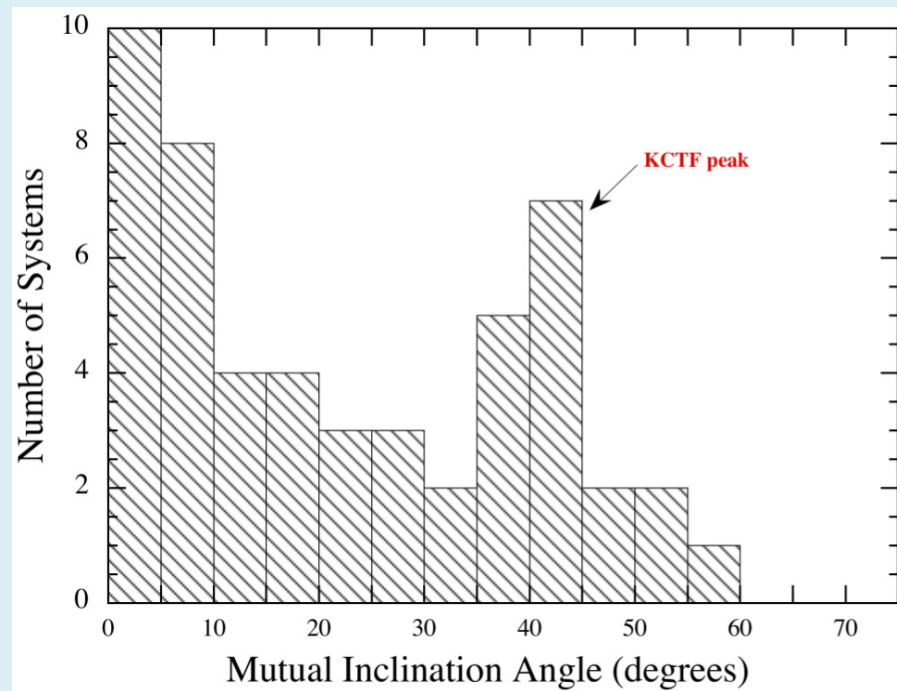


**Gaia will be first to fully measure  $f(P_{\text{in}}, P_{\text{out}})$  for OBA primaries**



# Triple Star Mutual Inclinations

Most compact solar-type triples with  $a_{\text{out}} < 50$  AU are coplanar ( $i < 40^\circ$ ), while wide tertiaries with  $a_{\text{out}} > 1,000$  AU have random orientations with respect to inner binary (Borkovits et al. 2016; Tokovinin 2017)



**Gaia will help constrain  $i_{\text{mutual}}(a_{\text{in}}, a_{\text{out}})$  for massive triples**



## Close Companions – Disk Fragmentation

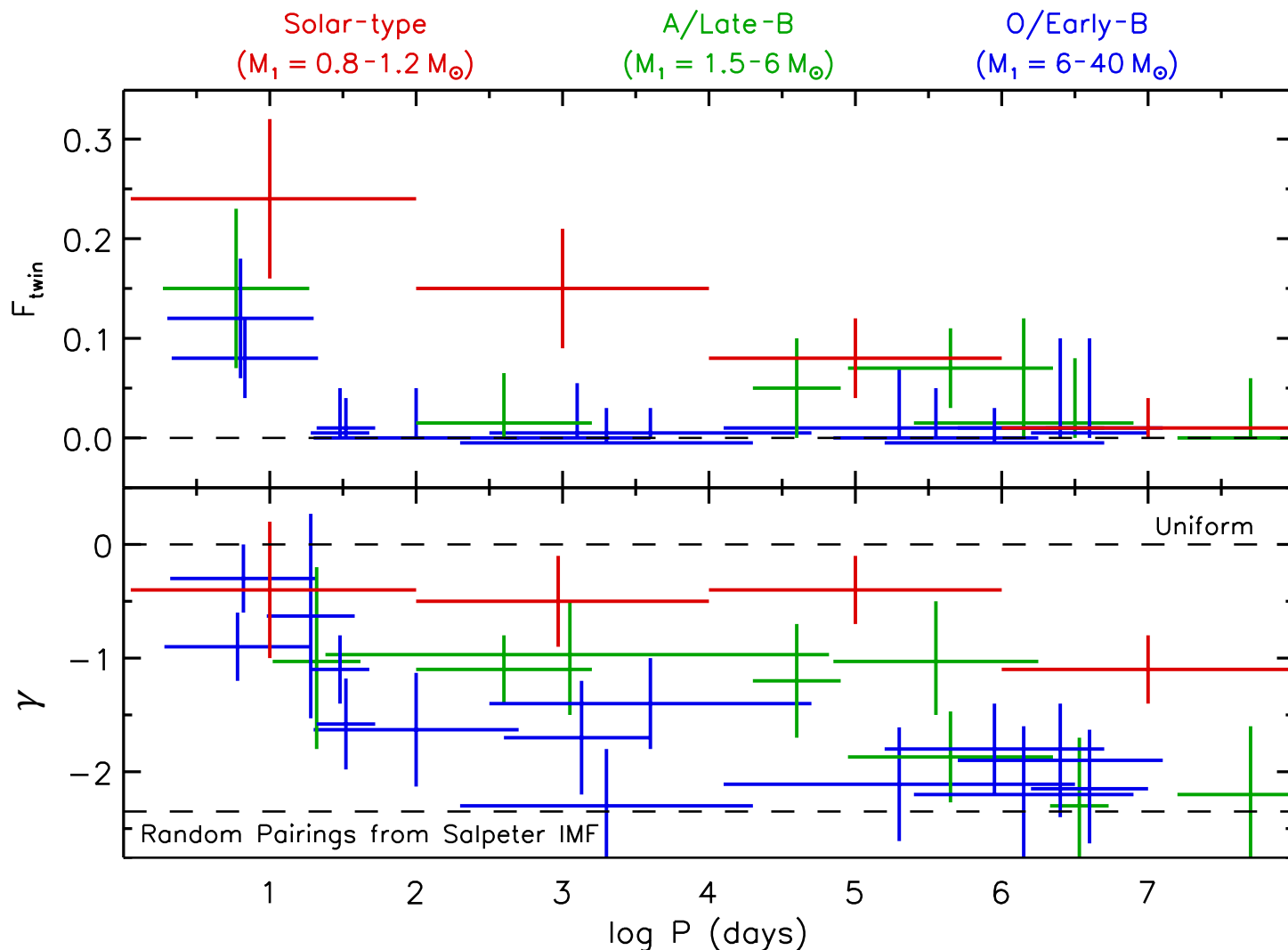
“A triple protostar system formed via fragmentation of a gravitationally unstable disk” (Tobin et al. 2016)



ALMA observations of L1448 IRS3B reveal coplanar tertiary accreting from disk at  $a_{\text{out}} \sim 100$  AU

# Mind your Ps and Qs: $f(P,q) \neq f(P)f(q)$ (Moe & Di Stefano 2017)

Excess fraction  
of twins with  
 $q > 0.95$

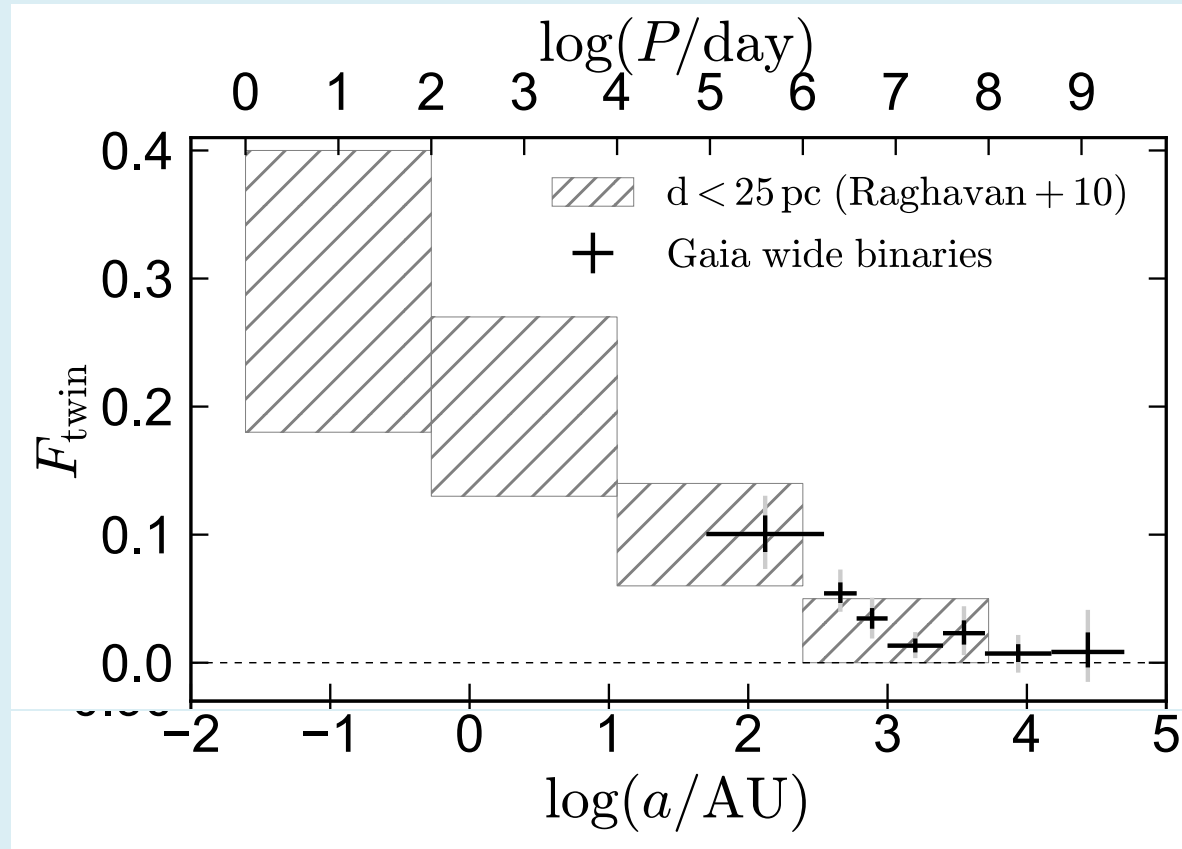


Power-law  
slope  
 $f \propto q^\gamma$

Very close binaries have uniform  $q$  distribution with excess twin fraction (disk fragmentation and accretion), wide binaries are weighted toward small  $q$  (core fragmentation), and there is an  $M_1$  dependent transition between these regimes.

Based on Gaia 200-pc sample of CPM binaries, El-Badry et al. (submitted; arXiv:1906.10128) confirmed wide binaries are weighted toward small  $q$ , but also found a small but statistically significant excess twin fraction extending out to a  $\sim 5,000$  AU.

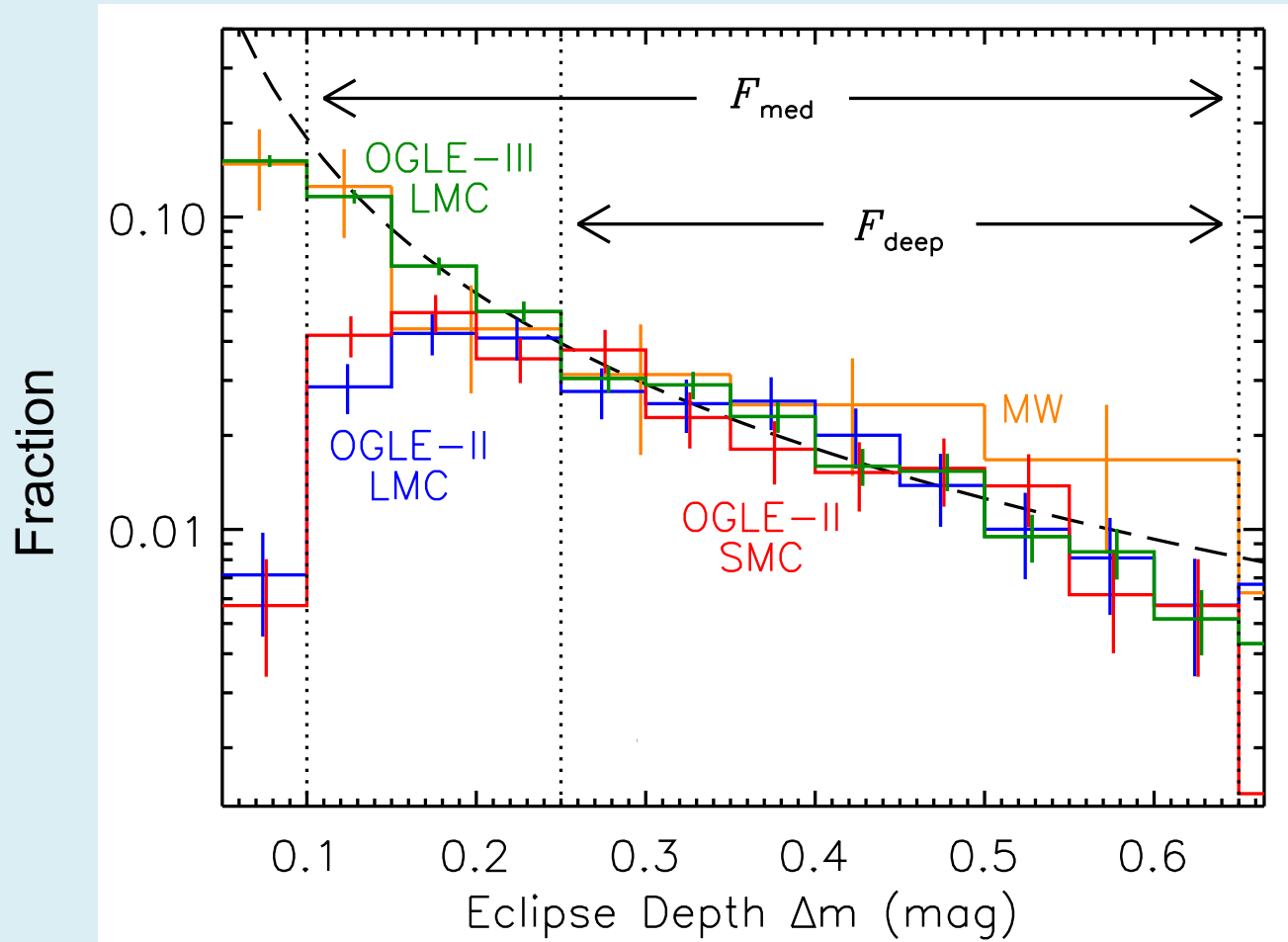
We concluded very wide twins initially formed in the disk within a  $< 200$  AU, but then were dynamically widened to a  $> 200$  AU in their dense birth clusters.



**Gaia DR3 spectroscopic and astrometric binaries will better constrain  $f_q(M_1, P)$ .**

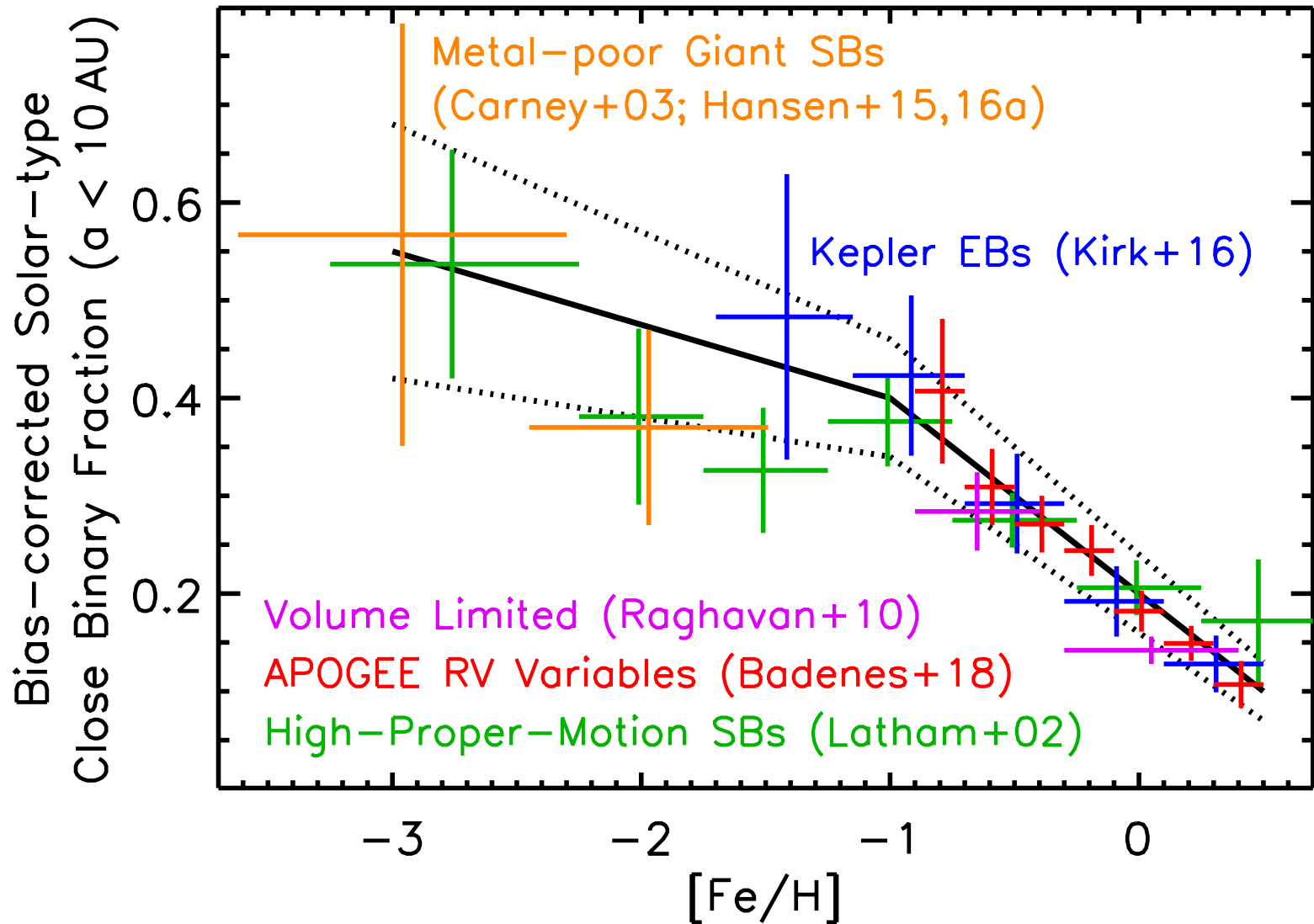
# Dependence on Metallicity

B-type EBs in the SMC, LMC, and MW (Moe & Di Stefano 2013)



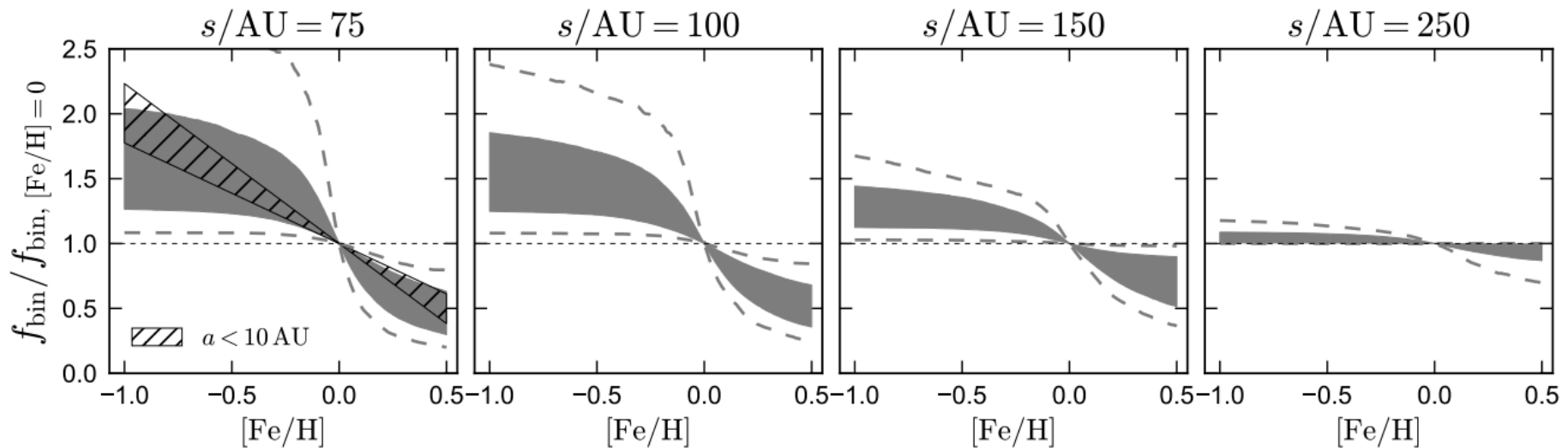
Properties of close massive binaries are invariant across  $-0.8 < [\text{Fe}/\text{H}] < 0.2$ .

Close binary fraction of solar-type stars decreases significantly with metallicity (Moe et al. 2019).



All five samples/methods provide consistent trend!

But imaging reveals the wide ( $a > 200$  AU) binary fraction of solar-type stars is metallicity invariant (Moe et al. 2019).



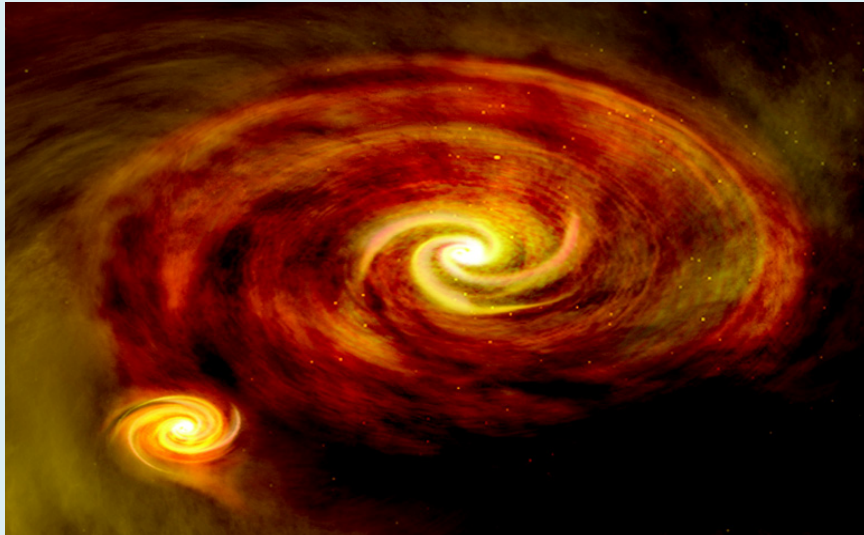
Utilizing Gaia common-proper-motion binaries with  $[\text{Fe}/\text{H}]$  measurements from wide-field spectroscopic surveys, El-Badry & Rix (2019) confirmed the metallicity dependence emerges below  $a < 200$  AU.

## Two Modes of Binary Star Formation (Moe et al. 2019)

Gravitational Instability and

Fragmentation of **Optically Thick Disks:**

$$Q_{\text{Toomre}} = c_s^2 \Omega / \pi G \Sigma = 3 \alpha c_s^3 / G \dot{M} < 1; \\ a < 100 \text{ AU}$$



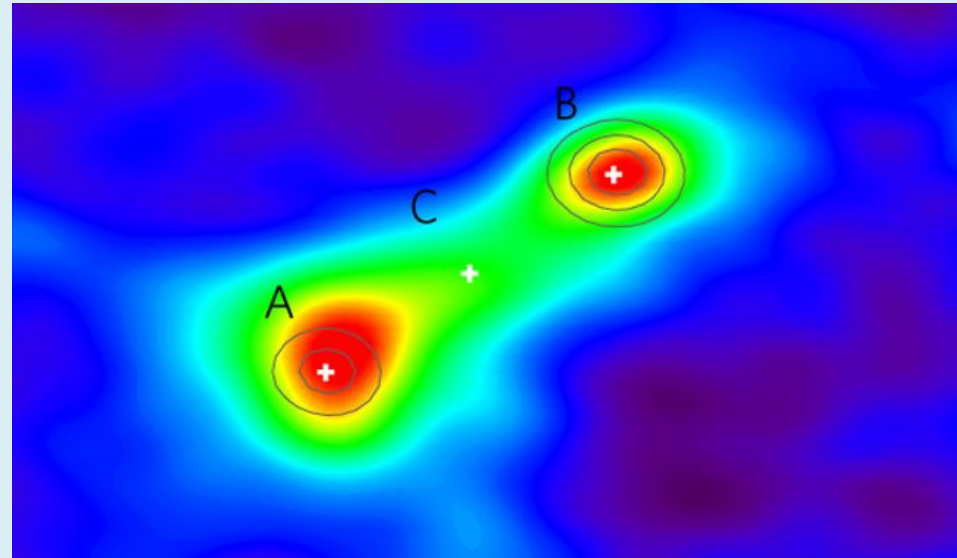
With decreasing  $[\text{Fe}/\text{H}]$ ,  
disks become less optically thick,  
become cooler, and fragment.

Massive disks of OB protostars have  
high accretion rates and always  
fragment, even at  $[\text{Fe}/\text{H}] = 0$

**Gaia DR3 will fill in gaps within  $f(M_1, P, Z)$  and explore dependence on  $X_i$**

Turbulent Fragmentation of  
**Optically Thin Molecular Cores:**

$$\text{Mach} = \sigma_v / c_s > 1; \quad a > 100 \text{ AU}$$

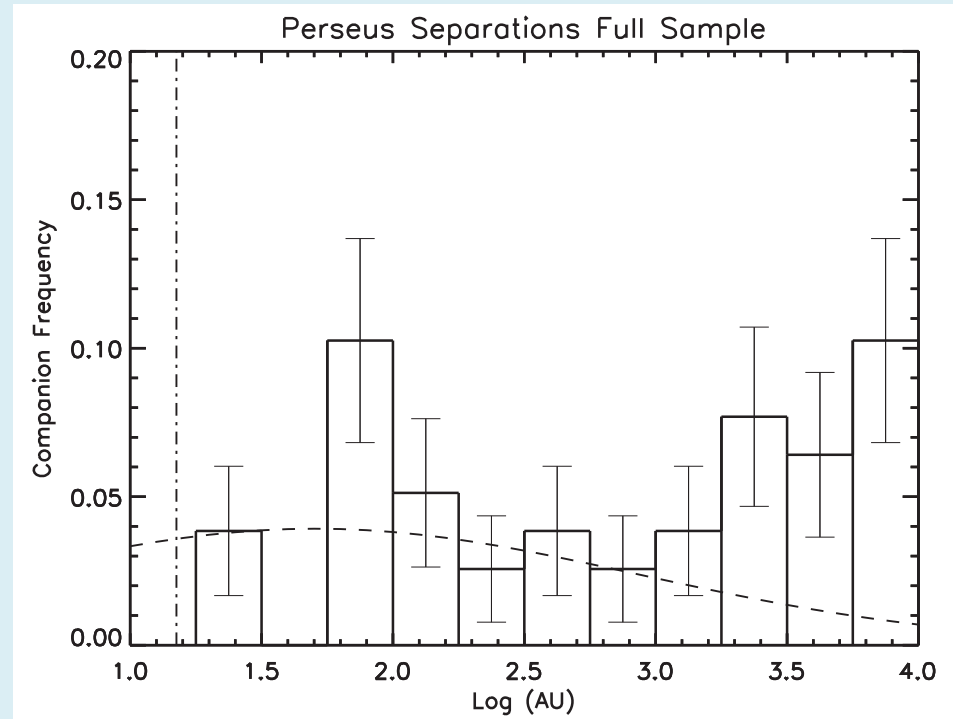
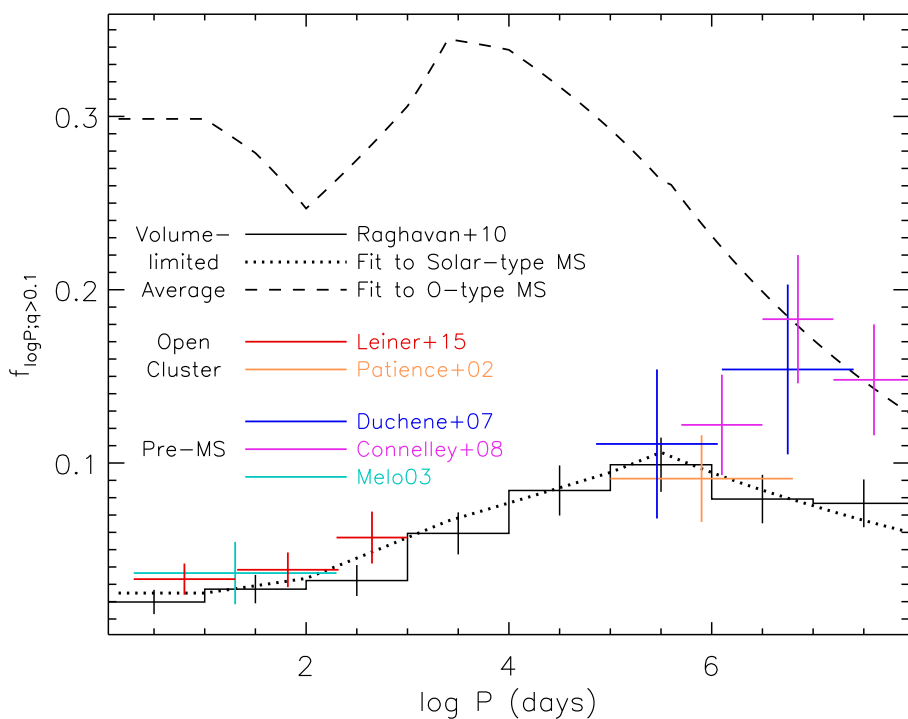


Independent of opacity (Bate+ 2019):  
wide binary fraction and IMF are  
metallicity invariant across  
 $-1.5 < [\text{Fe}/\text{H}] < 0.5$



# Pre-MS Binaries

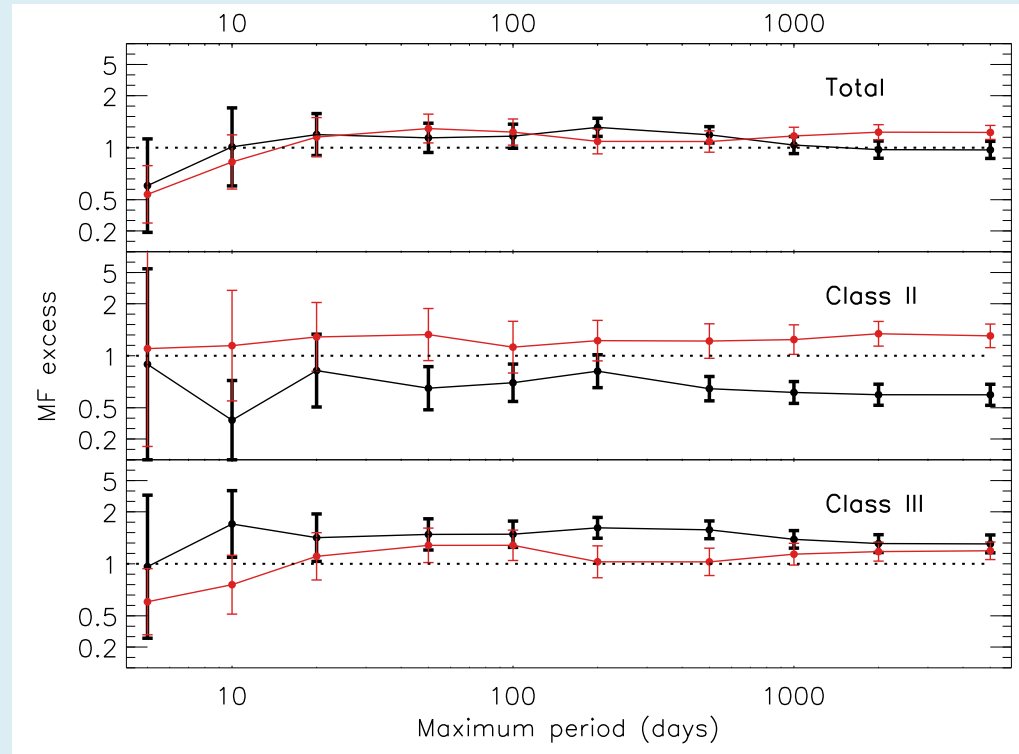
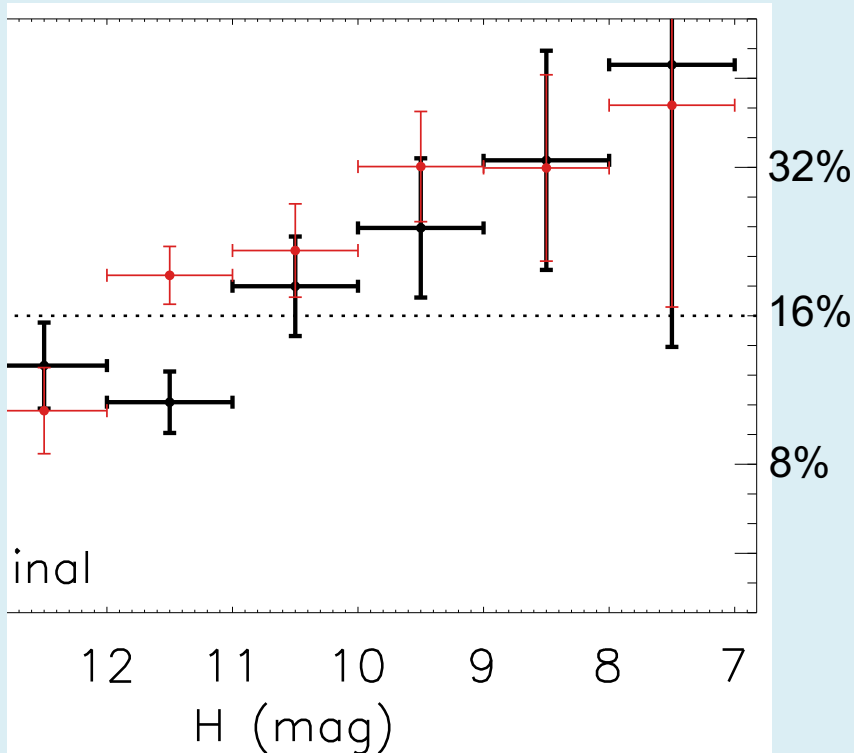
IR / radio observations of embedded class 0/I protostars reveal an excess of companions beyond a  $> 500$  AU, suggesting core fragmentation on large scales is efficient but then wide low-mass binaries are disrupted within  $\sim 0.5$  Myr (Duchene et al. 2007; Connelley et al. 2008; Tobin et al. 2016; Moe & Di Stefano 2017)



Kounkel et al. (2019) analyzed APOGEE spectra of  $\sim 5,000$  T Tauri stars, and discovered  $\sim 400$  binaries (SB2s from CCF and SB1s from RV variability).

Close binary fraction ( $a < 10$  AU) increases with luminosity (i.e.,  $M_1$ ), consistent with the field.

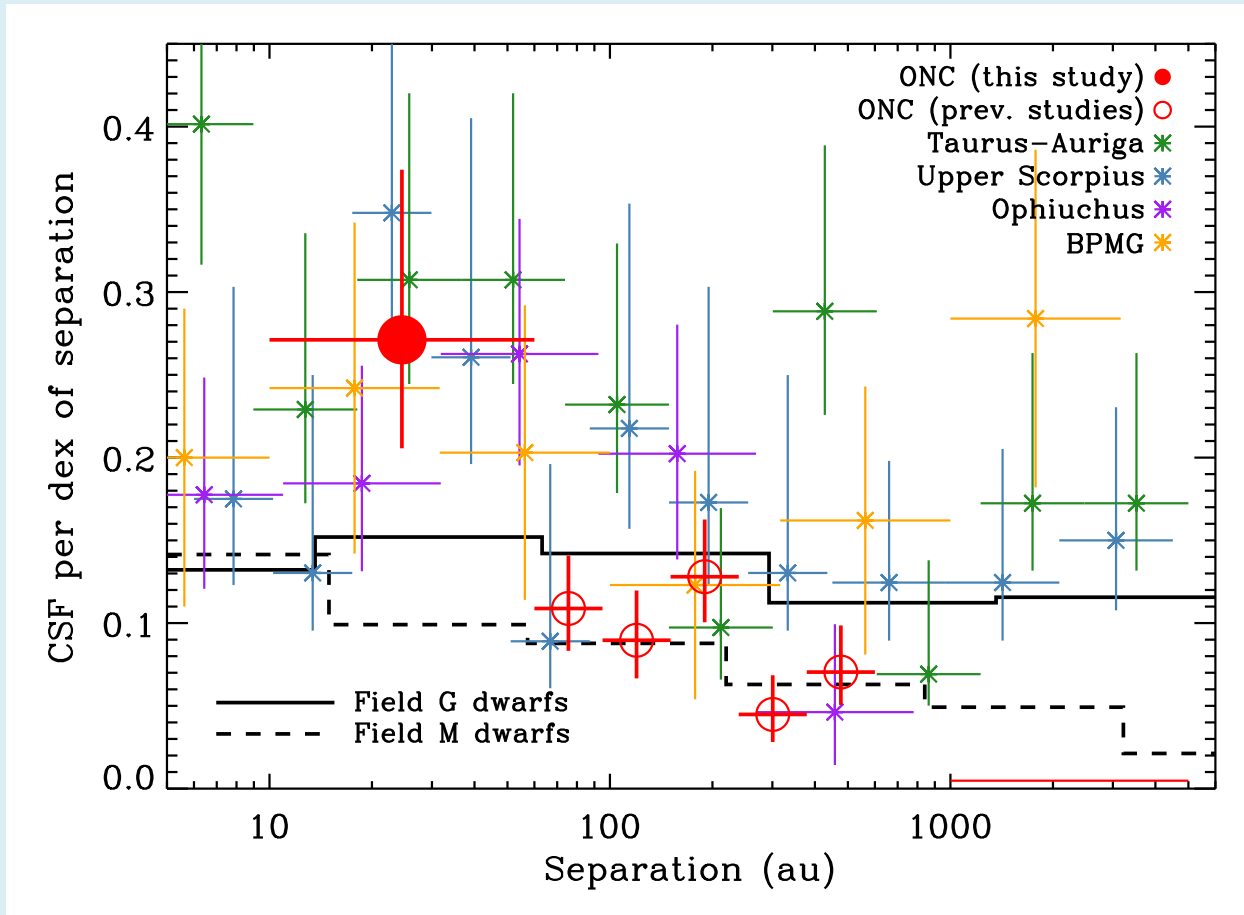
Separation distribution across  $a = 0.1 - 10$  AU matches field distribution.



Close binary properties of  $M_1 = 0.3 - 3 M_{\odot}$  primaries set by  $\sim 1$  Myr!

AO and sparse aperture masking reveal an excess of young T Tauri binaries across  $a = 10 - 60$  AU compared to the field (Duchene et al. 2018).

The consistency below  $a < 10$  AU and across  $a = 60 - 500$  AU but large excess across  $a = 10 - 60$  AU, even in Orion, is a major mystery!



Perhaps Gaia can help resolve discrepancy / discontinuity in  $f(P, \tau, n)$ ?

# Compact Remnant Companions to MS Stars

Regulus: a rapidly rotating B8IV star;  
P = 40 day SB1, likely a WD companion

Census of confirmed WD companions closely orbiting BAFG stars incomplete beyond  $d > 10$  pc (Holberg et al. 2016); **Gaia will help**

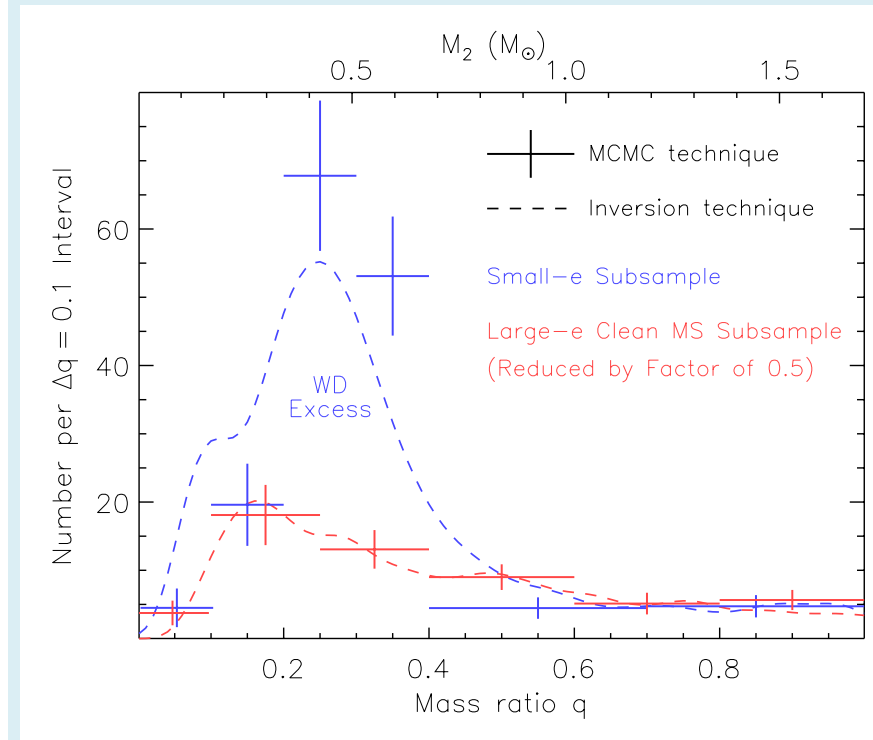
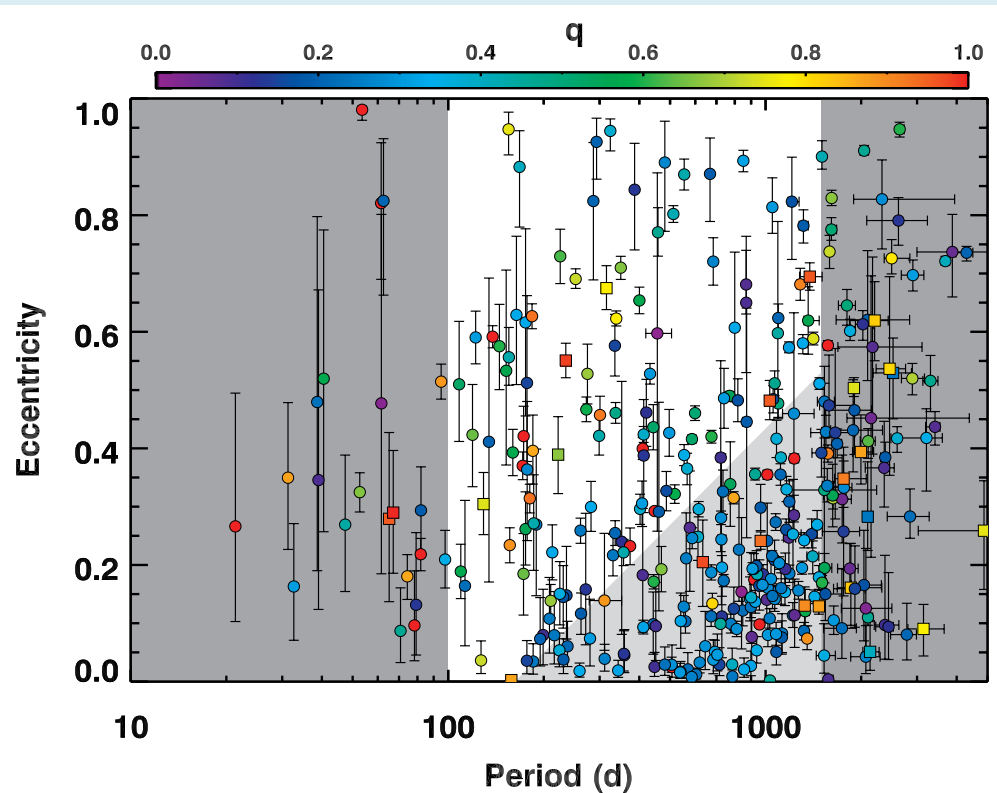
After correcting for incompleteness,  $11\% \pm 3\%$  of field solar-type stars have WD companions, i.e.,  $\sim 20\%$  of companions are WDs, and  $30\% \pm 10\%$  of SB1s have WD companions (Moe & Di Stefano 2017)



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$\sim 30\%$  of O stars are the products of binary evolution (de Mink et al. 2015), and  $\sim 20\%$  of OB “primaries” are actually the companions in which the true primaries have already evolved into NSs or BHs (Moe & Di Stefano 2017)

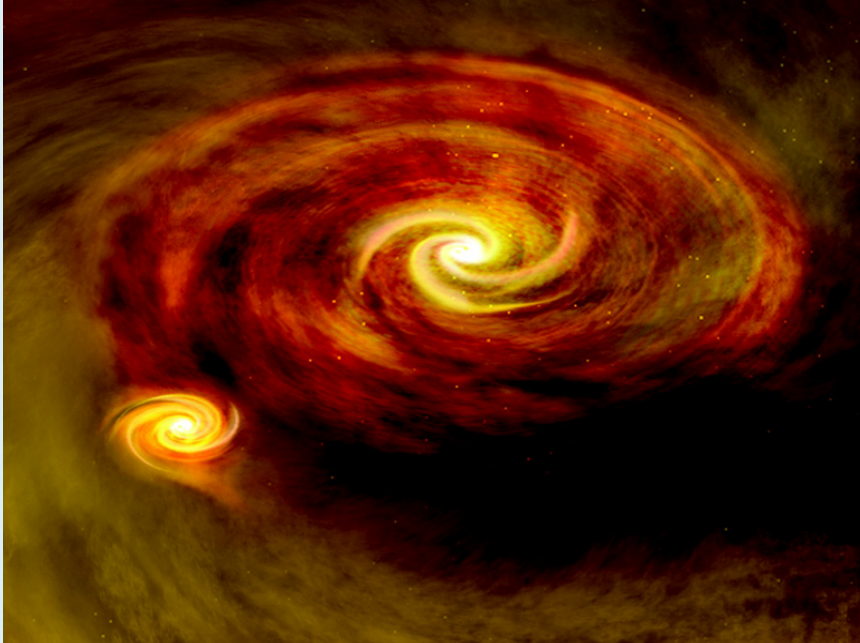
Phase modulation of Kepler pulsating  $\delta$  Scuti stars (older A/F dwarfs) reveal binary companions across  $a = 0.5 - 5$  AU,  $22\% \pm 6\%$  of which are WDs with small eccentricities (Murphy, Moe et al. 2018)



# Overall Theme

## Disk Fragmentation:

Close binaries with  $a < 100$  AU



Increases with  $M_1$ .

Compact coplanar triples.

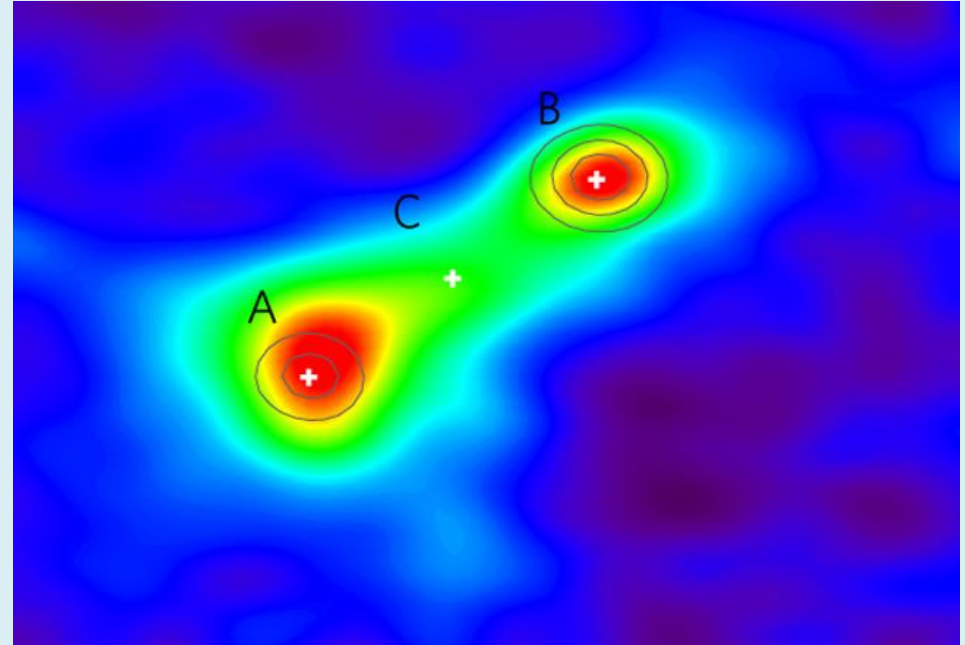
Uniform  $q$  & excess twins.

Decreases with  $[Fe/H]$ .

Independent of  $\tau$  and  $n$ .

## Core Fragmentation:

Wide binaries with  $a > 100$  AU



Independent of  $M_1$ .

Wide tertiaries randomly oriented.

Weighted toward  $q = 0.3$  & few twins.

Independent of  $[Fe/H]$ .

Decreases with  $\tau$  and  $n$ .

# Conclusion

Multiplicity statistics constitute a complicated parameter space:

$f(M_1, M_2, P, e, [MS, BD, WD, NS, BH], [M_3, P_{out}, i_{mut}], [Z, X_i], [\tau, n])$

Gaia will explore new regions of this parameter space, providing new insights into binary star formation and evolution.